Chemistry 3830

Symmetry

Symmetry Elements and Operations

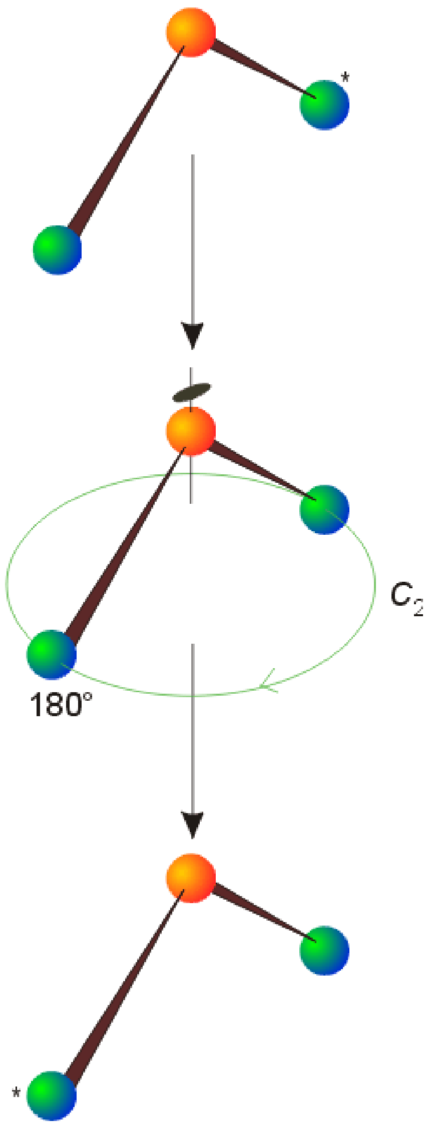
Symmetry Operation	Symmetry Element	Symbol
Identity		E
Proper rotation	Rotation axis	C_n
Reflection	Mirror plan	σ
Inversion	Inversion centre/ centre of symmetry	i
Improper rotation	Improper rotation axis	S_n

Schoenflies notation

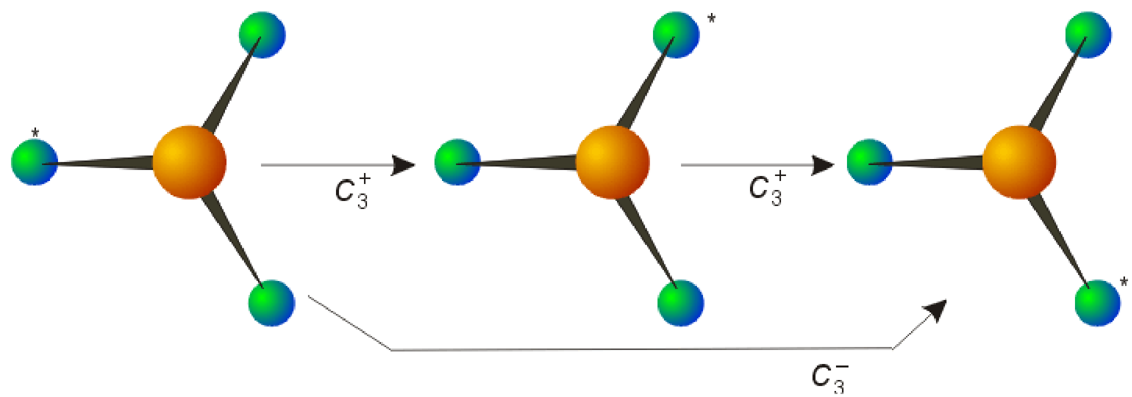
(Proper) Rotation, C_n

- Rotation by 360°/n

C_2

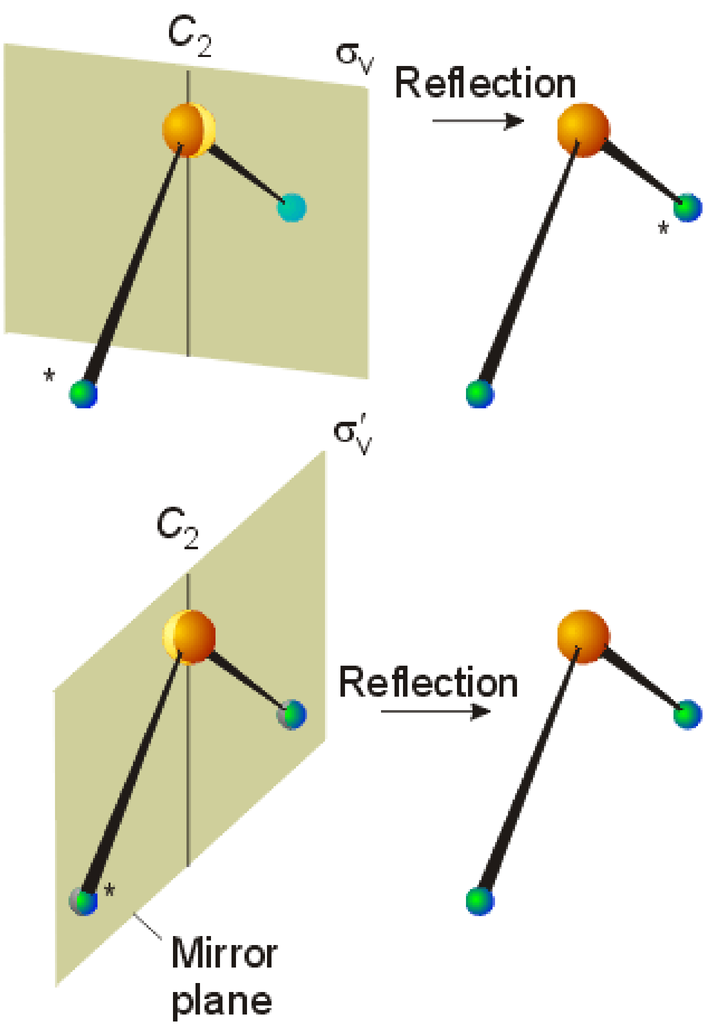


C_3



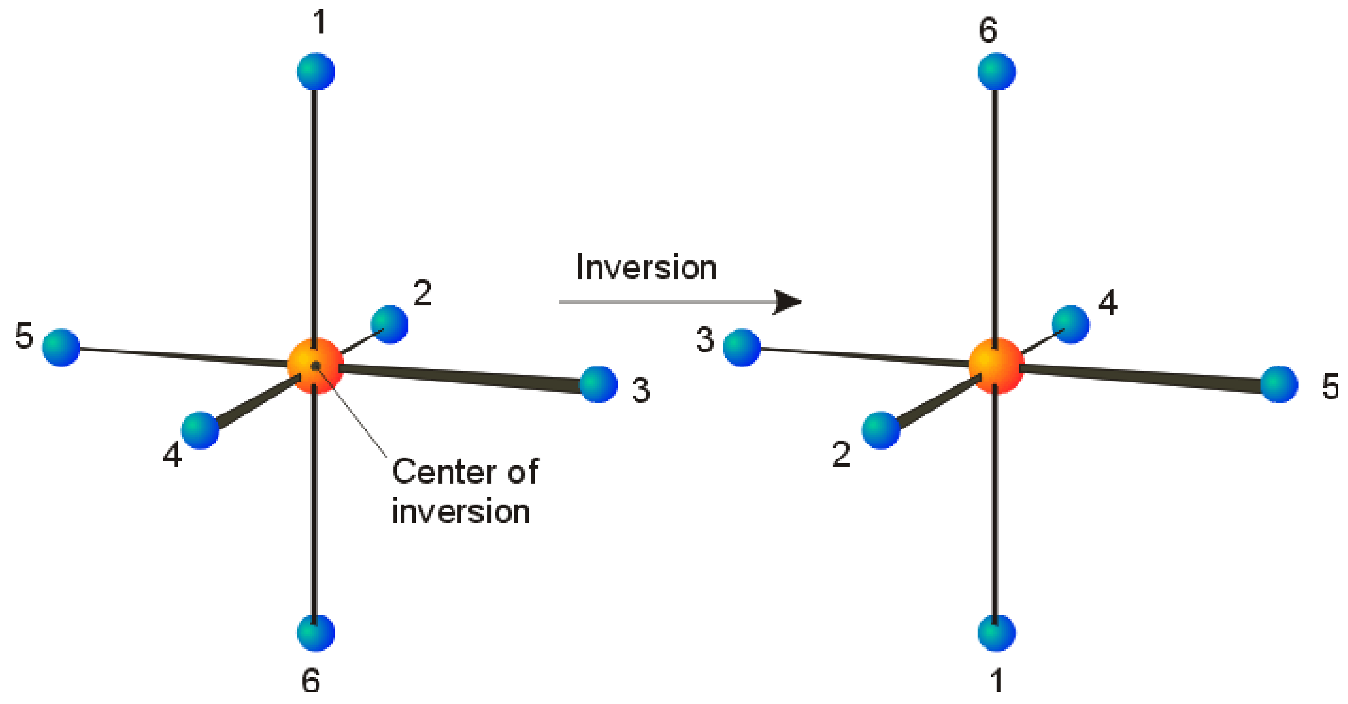
Reflection, σ

Example: H_2O



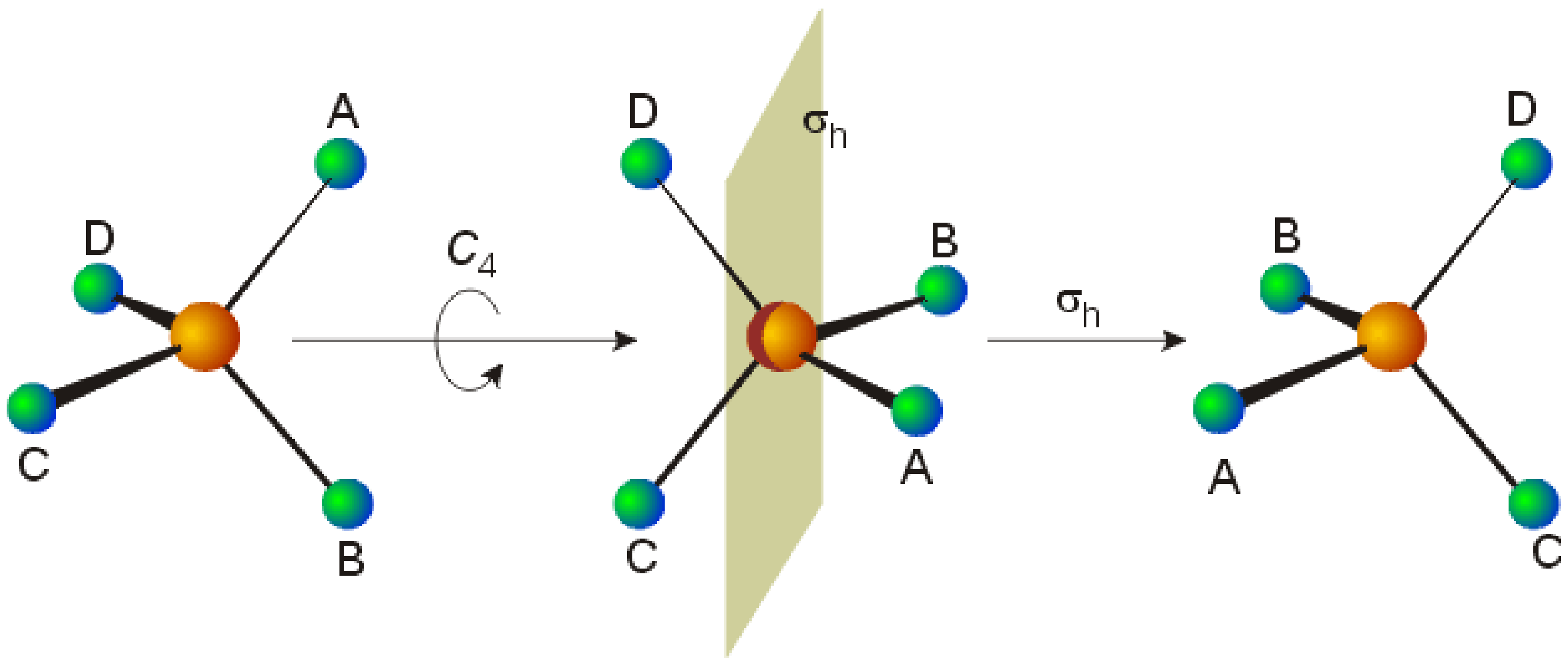
Inversion Centre

Example: SF_6

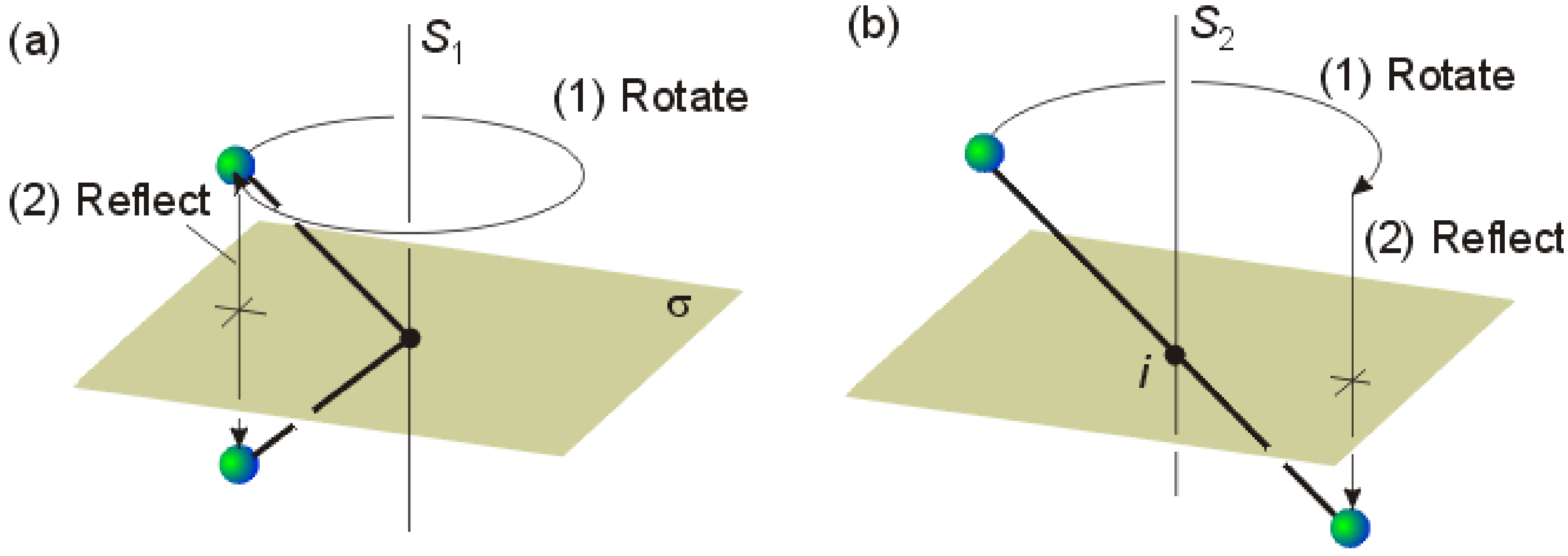


Improper Rotation (Axis), S_n

Example: CH_4

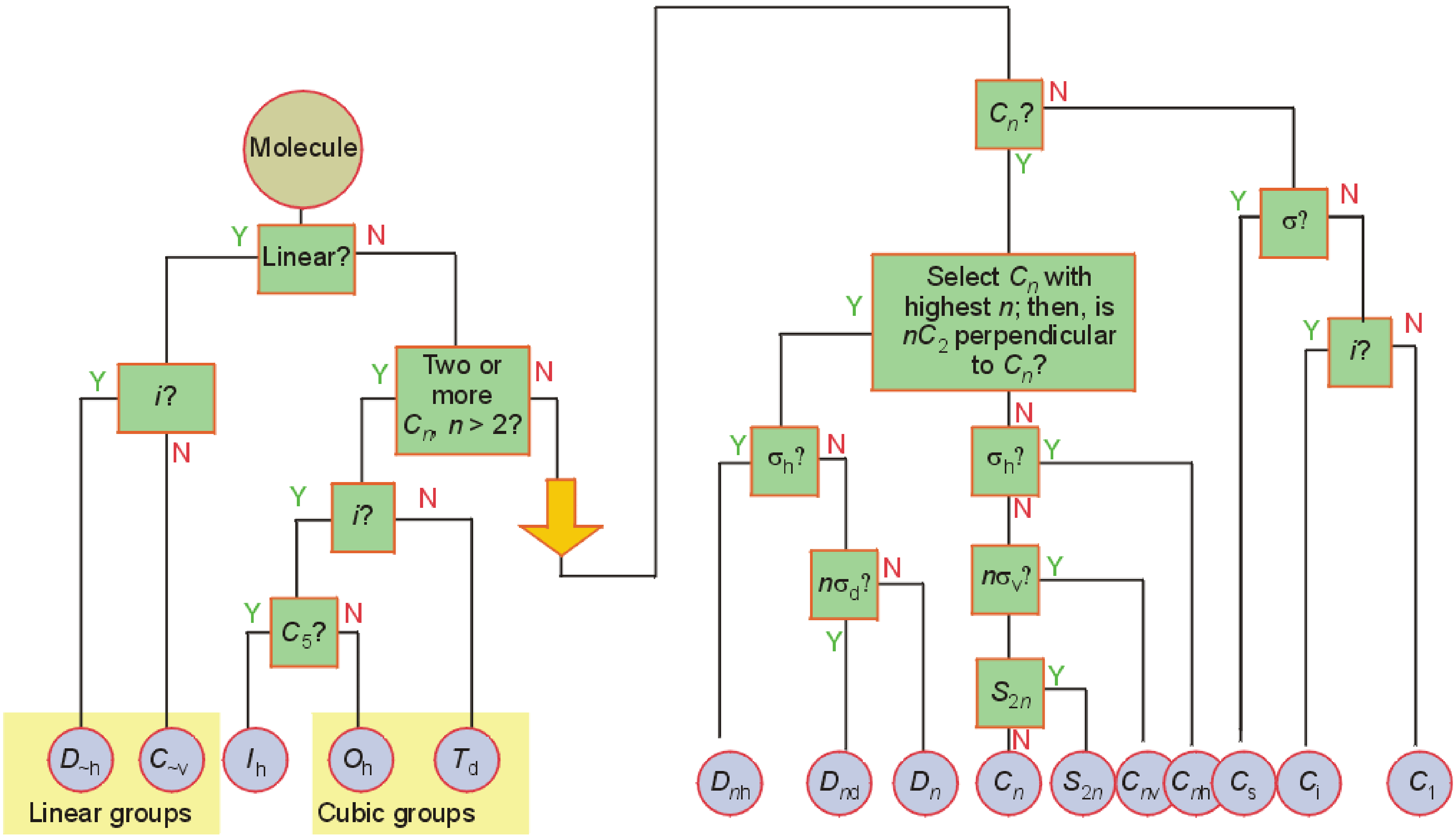


Improper Rotation (Axis), S_n



- You will not find S_1 or S_2 axes.

Point Groups



Point Groups

Polar point groups:

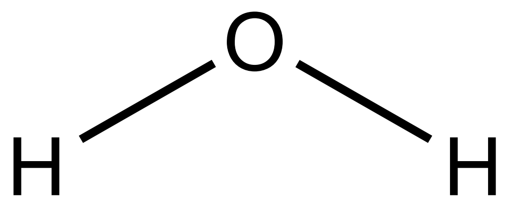
- must **not** belong to a D group of any kind, nor T_d, O_h or I_h

Chiral point groups:

- must **not** possess an S_n axis

(therefore, no mirror planes, nor an inversion centre, which are equivalent to S_1 and S_2, respectively).

Character Tables



C_{2v}	E	C_2	$\sigma_v(xz)$	$\sigma_v(yz)$		
A_1	1	1	1	1	z	x^2, y^2, z^2
A_2	1	1	-1	-1	R_z	xy
B_1	1	-1	1	-1	x, R_y	xz
B_2	1	-1	-1	1	y, R_x	yz

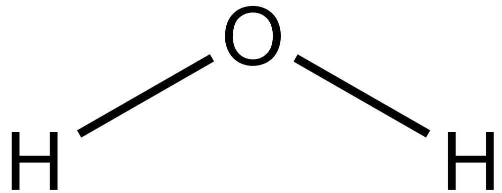
Symmetry operations

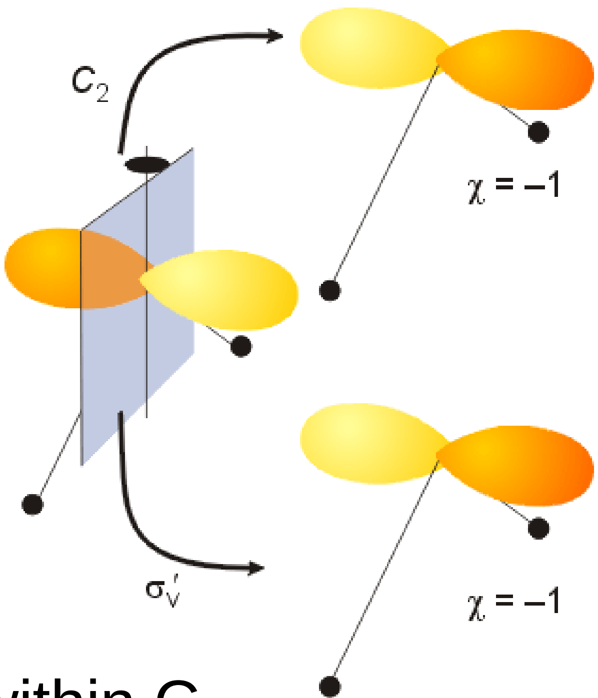
Symmetry species = Mulliken labels

Characters = χ

Character Tables

C_{2v}	E	C_2	$\sigma_v(xz)$	$\sigma_v(yz)$		
A_1	1	1	1	1	z	x^2, y^2, z^2
A_2	1	1	-1	-1	R_z	xy
B_1	1	-1	1	-1	x, R_y	xz
B_2	1	-1	-1	1	y, R_x	yz

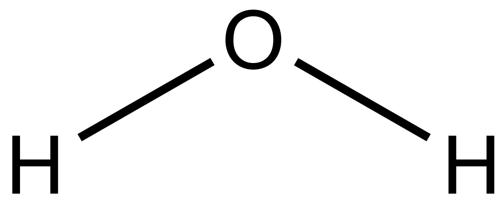




- The p_x orbital transforms as B_1 within C_{2v}

Character Tables

C_{2v}	E	C_2	$\sigma_v(xz)$	$\sigma_v(yz)$		
A_1	1	1	1	1	z	x^2, y^2, z^2
A_2	1	1	-1	-1	R_z	xy
B_1	1	-1	1	-1	x, R_y	xz
B_2	1	-1	-1	1	y, R_x	yz



Character Tables

The cubic groups (continued)

O_h ($m3m$)	E	$8C_3$	$6C_2$	$6C_4$	$3C_2$ ($=C_4^2$)	i	$6S_4$	$8S_6$	$3\sigma_h$	$6\sigma_d$	$h = 48$	
A_{1g}	1	1	1	1	1	1	1	1	1	1		$x^2+y^2+z^2$
A_{2g}	1	1	−1	−1	1	1	−1	1	1	−1		
E_g	2	−1	0	0	2	2	0	−1	2	0		$(2z^2-x^2-y^2, x^2-y^2)$
T_{1g}	3	0	−1	1	−1	3	1	0	−1	−1	$(R_x, R_y R_z)$	
T_{2g}	3	0	1	−1	−1	3	−1	0	−1	1		(xy, yz, zx)
A_{1u}	1	1	1	1	1	−1	−1	−1	−1	−1		
A_{2u}	1	1	−1	−1	1	−1	1	−1	−1	1		
E_u	2	−1	0	0	2	−2	0	1	−2	0		
T_{1u}	3	0	−1	1	−1	−3	−1	0	1	1	(x, y, z)	
T_{2u}	3	0	1	−1	−1	−3	1	0	1	−1		

Character Tables

The cubic groups (continued)

O_h ($m3m$)	E	$8C_3$	$6C_2$	$6C_4$	$3C_2$ ($=C_4^2$)	i	$6S_4$	$8S_6$	$3\sigma_h$	$6\sigma_d$	$h = 48$	
A_{1g}	1	1	1	1	1	1	1	1	1	1		$x^2+y^2+z^2$
A_{2g}	1	1	−1	−1	1	1	−1	1	1	−1		
E_g	2	−1	0	0	2	2	0	−1	2	0		$(2z^2-x^2-y^2, x^2-y^2)$
T_{1g}	3	0	−1	1	−1	3	1	0	−1	−1	(R_x, R_y, R_z)	
T_{2g}	3	0	1	−1	−1	3	−1	0	−1	1		(xy, yz, zx)
A_{1u}	1	1	1	1	1	−1	−1	−1	−1	−1		
A_{2u}	1	1	−1	−1	1	−1	1	−1	−1	1		
E_u	2	−1	0	0	2	−2	0	1	−2	0		
T_{1u}	3	0	−1	1	−1	−3	−1	0	1	1	(x, y, z)	
T_{2u}	3	0	1	−1	−1	−3	1	0	1	−1		

Mulliken labels: A, B = non-degenerate
E = doubly degenerate
T (or F) = triply degenerate

g = gerade = symmetric with respect to i.
u = ungerade = antisymmetric with respect to i.